

REVIEWS

A Review on Neural Dynamics for Robot Autonomy

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ABSTRACT

Exploiting neural networks to solve control problems of robots is becoming commonly and effectively in academia and engineering. Due to the remarkable features like distributed storage, parallelism, easy implementation by hardware, adaptive self-learning capability, and free of off-line training, the solutions of neural networks break the bottlenecks of serial-processing strategies and methods, and serve as significant alternatives for robotic engineers and researchers. Especially, various types and branches of recurrent neural networks (RNNs) have been sequentially developed since the seminal works by Hopfield and Tank. Successively, many classes and branches of RNNs such as primal-dual neural networks (PDNNs), zeroing neural networks (ZNNs) and gradient neural networks (GNNs) are proposed, investigated, developed and applied to the robot autonomy. The objective of this paper is to present a comprehensive review of the research on neural networks (especially RNNs) for control problems solving of different kinds of robots. Specifically, the state-of-the-art research of RNNs, PDNNs, ZNNs and GNNs in different robot control problems solving are detailedly revisited and reported. The readers can readily find many effective and valuable solutions on the basis of neural networks for the robot autonomy in this paper.

Key Words: Neural dynamics, Robot autonomy, Recurrent neural networks, Zeroing neural networks, Primal-dual neural networks, Gradient neural networks

1. INTRODUCTION

Neural networks (or termed artificial neural networks) are simple systems that are composed of many connected neurons to simulate the structure of human brain.^[1-5] Neural networks usually possess the characteristics of adaptivity, nonlinearity, parallelism and distributed storage, which can be used to solve the complicated problems that can not be solved by other approaches.^[6-9] Specifically, the applications of neural networks including (but not limited to) the pattern classification,^[10,11] deep learning,^[12,13] approximation and prediction,^[14,15] image processing,^[16,17] machine learning,^[18,19] optimization and computation,^[20,21] complex system control^[22-24] (including the robot system control).^[25,26] Due to the extensive and significant applications of neu-

ral networks, the development and investigation of neural networks have become common and heated topics for the researchers in biology, mathematics, physics, and computer science.^[27-40]

According to different standards of classification, neural networks can be divided into different categories. From the point of topology, neural networks can be divided into feed-forward neural networks (FNNs)^[41-44] and recurrent neural networks (RNNs).^[45-65] Note that the FNNs are the hierarchical structure with each layer divided by the function as the input-layer, the hidden-layer, and the output-layer. Each neuron in FNNs receives the inputs from the previous layer, and exports the information to the next layer. The information is transmitted with a fixed (or to say, single) direction without

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feedback.^[66] Differing from the FNNs, the RNNs are those neural networks that possess the feedback connections of each network layers.^[67] The network structure of RNNs is more complicated than the one of FNNs. Specifically, each neuron in the RNNs exports outputs to other neurons via the connected synapses. At the same time, each neuron in the RNNs receives inputs from other neurons via the connected synapses. The input information lies on the initial states of RNNs. Then, real-time states of RNNs vary adaptively. Finally, the RNNs converge to the equilibrium states (or termed steady states), and the steady states are the outputs of the RNNs. Recently, many special classes and branches of RNNs have been developed and investigated, such as primal-dual neural networks (PDNNs),^[68–76] Zhang neural networks [or termed zeroing neural networks (ZNNs)^[77–106] and gradient neural networks (GNNs).^[107–114] Note that the ZNN is a special class and branch of RNNs, which is originated and extended from the research of Hopfield neural networks. The ZNNs have been proposed developed, and investigated as a systematic as well as efficient approach to solve different dynamical engineering problems in real time since 2001.^[68,69] The applications, especially the applications in robot autonomy, of those RNNs have become interesting issues for researchers and engineers.^[115–120]

With the national industrialization, robot systems play an increasingly significant role in applications of modern en-

gineering, life services as well as numerous fields. Robot systems have been widely used in engineering applications for cutting, welding, painting and assembly, etc. In addition, they have been widely used in life services for medical assistance, rescue, etc. Generally speaking, robot systems can be divided into serial robot manipulators (e.g., the Baxter robot^[121–127]), parallel robot manipulators (e.g., the Stewart platform^[128–130]), mobile platform robots (e.g., the Mobile Kinova manipulator^[131,132]), multirobot systems (e.g., the multiple redundant manipulators^[133,134]), flying robots (e.g., the unmanned aerial vehicle^[135]) and exoskeleton robots (e.g., the knee exoskeleton^[136]). One significant issue in the research of robot systems is the motion planning and control problem. Up to now, a large number of effective approaches for robot systems have been creatively proposed and effectively employed, such as the neural networks approach,^[137] the active control approach,^[138] the robust control approach,^[139] the optimal control approach,^[140] etc. In this survey, we aim to provide a comprehensive review on the research of neural networks (or to say, neural dynamics) in robot autonomy. Specifically, the state-of-the-art research of RNNs, PDNNs, ZNNs and GNNs in different robot control problems solving are detailedly revisited and reported, with the typical applications shown in Figure 1. The readers can readily find many referenced and valuable solutions on the basis of neural networks for the robot autonomy in this paper.

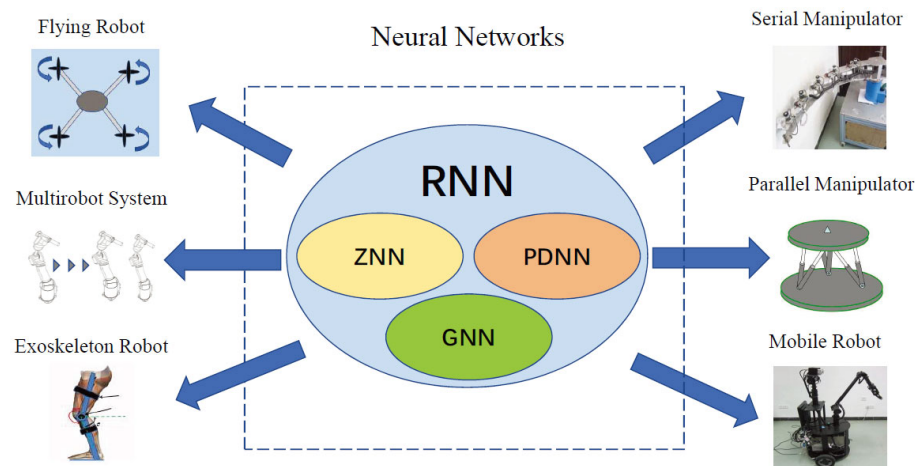


Figure 1. Applications of neural networks in robot autonomy

2. RNN IN ROBOT AUTONOMY

In the past three decades, by leveraging the advantages of parallelism and adaptivity as well as the free of off-line learning, the RNNs have received considerable investigation in robot autonomy. For example, Zhang and Zhang^[116] effectively solved the joint-angle as well as joint-velocity drift problems during the repeated motion of robot manipulators, by propos-

ing a drift-free method in acceleration-level limited by the linear equality constraint. Noth that the effectiveness was detailedly analysed on the basis of the theory of a second-order system. Such a method proposed in^[116] is afterwards formulated as the quadratic programming (QP), and solved by corresponding RNNs. In,^[141] a novel dual-manipulator repetitive motion generation strategy was proposed by the

neural dynamics approach to handle and address a joint-drift problem of the humanoid robot. Specifically, based on such a neural dynamics approach, a performance index for repetitive motion was effectively utilized in,^[141] and then such a performance index was integrated as the QP formulation with the time-varying constraints. Specifically it was named as the time-varying constrained scheme. Such a scheme can effectively produce a repeated motion of two manipulators of the humanoid robot. Besides, it also can control two manipulators to move to a desired position, which was finally solved by a RNN to achieve the optimal solutions. In addition, Zhang et al.^[142] employed a virtual plane method to produce an analytical solution for the motion of the robot head. Then, a QP-based method was exploited to formulate the coordinated dual-arm motion. By utilizing a simplified RNN, the optimal solution was finally found. Mohammed and Li^[128] investigated and formulated the kinematics control for the Stewart platform as the QP with constraint. Note that Karush-Kuhn-Tucker conditions of problem were attained via considering the primal one in dual space, and afterwards an RNN was developed to handle such an optimization problem. Detailed theoretical analyses in^[128] prove the global convergence of such a neural network to the optimal solution according to the defined performance index. In 2017, Li et al.^[143] identified two major limitations of the RNN solutions for the robot manipulator autonomy, that is the accumulation of position error as well as the convex restriction of projection set. The proposed method in reference^[143] overcame the above mentioned limitations by developing modified neural network models, which enables nonconvex sets of projection operations, and the position error will not accumulate over time under the influence of the noise. Differing from many works the corresponding RNNs are utilized to address time sequences, the corresponding method has the advantages of model-based as well as training-free. It makes it feasible to obtain rapid tracking of reference signals. In,^[144] three different RNNs and three different numerical methods was investigated, developed, and compared to solve a repetitive motion planning (RMP) scheme for remedying joint-drift problems of redundant robot manipulators. Three RNNs presented in^[144] are recurrent and real time, and they do not need to be trained in advance. Li et al.^[145] proposed a novel RNN to handle the redundancy of robots for efficient kinematics problem under the influence of polynomial-type noises. By taking advantage of high-order derivative properties of polynomial-type noises, the devised neural network model was developed to remove the negative influence of noises, and regain the effective tracking of reference trajectories in high accuracy. To solve the joint drift phenomenon that might lead to the failure of the given task, or even worse, the damage of the

robot, a finite time varying parameter RNN was introduced and developed in.^[146] A QP-type joint drift-free solution was proposed, which consists of an optimization performance index and a velocity-level kinematics equation. Note that a feedback information was added to the kinematics equation as a constrained equality. In addition, a novel joint drift-free solution considering feedback was achieved. Then, a novel RNN model was developed to solve the proposed scheme, and the related finite-time convergence theorem was given. Specifically, the superiorities of the proposed RNN in^[146] the real-time computation, the exponential convergence, as well as the capacity to remove initial errors. Moreover, Jin et al.^[147] revisited the existing RNN and its related models for addressing zero-finding, such as the inversion of matrix, with time-varying parameters from control perspective, and then formulated as a control-theoretical framework. Afterwards, the constraints of activated functions of RNN and the related models were presented, and handled by taking advantage of control techniques. Besides, the gradient-based RNN, as a typical solution for zero-finding, were represented to handle the dynamic issues in manners free of errors as well as matrix inversions. The research in^[147] provided a systematic and general method on using control techniques to develop the corresponding RNN and the related models for robustly as well as accurately handling algebraic equations and the robot autonomy problems. More detailed research by utilizing the RNNs with application to robot autonomy can also be referred in the state-of-the-art works.^[148-150]

3. PDNN IN ROBOT AUTONOMY

Many special classes and branches of RNNs have been introduced and investigated for the robot kinematic as well as dynamic autonomy, e.g., the Lagrangian neural networks and the PDNNs.^[151] In particular, Zhang et al.^[68] proposed a dual neural network (i.e., a special case of PDNNs) for the bi-criteria kinematics issue of robot manipulators. In order to eliminate discontinuity of minimum infinity-norm solutions, the kinematics control issue was reformulated as the bi-criteria of infinity and Euclidean norms in.^[68] Note that physical constraints, like joint-angle limit as well as joint-velocity limits were incorporated in the kinematics control solution. Such a dual neural network was proven to converge to the optimal solutions globally in a bi-criteria sense, and was illustrated to be effective for the PA10 robot autonomy in.^[68] In addition, a dual neural network was developed in^[69] for the real-time joint-torque optimization of redundant robot manipulators corresponding to the global energy minimization of robot manipulators. Differing from existing computational schemes on the inverse kinematics, a dual neural network was introduced at acceleration level to handle

redundancy issue of limited joint-range robots. Note that such a dual neural network possesses a quite simple structure with one layer of neurons. It was proved to converge to the optimal solutions globally as well as exponentially in.^[69] Such a dual neural network was finally simulated with a PUMA 560 robot manipulator to substantiate effectiveness. In 2004, Zhang and Wang^[71] proposed and developed a new dual neural network with application to kinematics autonomy of redundant robot manipulators with the ability of obstacle avoidance. Note that the requirement of obstacle avoidance was represented by the dynamical inequality limits, an improved problem formulation was presented in.^[71] On the basis of the above improved problem formulation, a novel dual neural network was introduced for solving real-time collision-free problem of inverse kinematics. Such a proposed new dual neural network was applied to the autonomy of a PA10 robot manipulator with a point obstacle as well as a window-shaped obstacle. In 2007, the neural computation of real-time solution of the matrix-inverse problems was investigated in.^[152] The basic concepts of primal neural network and power-sigmoid activation function were thus formally proposed for the general neural computation of matrix inverse. Different activation functions were examined and presented in^[152] for the superior convergence as well as robustness of the system involved. In addition to the singular case, the reference^[152] investigated a robotic example, that is, inverse kinematic autonomy of redundant robots by using real-time pseudo-inverse computation. Chen and Zhang^[153] proposed a novel minimum jerk norm solution with the obstacle-avoidance constraint with the application to a redundant manipulator, of which its joint jerks keep bounded for the human-friendly robot autonomy. For the aim of superior tracking performance of the redundant manipulator, the presented jerk bounded MJN solution in^[153] was further improved by feedback information. Moreover, the effectiveness of the obstacle avoidance of the solution was proven by a variable-magnitude escape-jerk theorem. Then, the proposed solution was formulated into the dynamical QP which is then handled by a special kind of PDNNs. In 2017, a hybrid multi-objective (HMO) solution was novelly developed in^[76] to simultaneously achieve four objectives, i.e., the specified main task for end-effector, obstacle avoidance, joint-physical limits avoidance, as well as repetitive motion of robot manipulators. Afterwards, such an HMO solution in^[76] was formulated into a dynamical QP with the optimal solution of the dynamical QP problem found by a special kind of PDNNs and also by a numerical algorithm implemented on the computer. In,^[154] a jerk-level synchronous repetitive motion solution was introduced to handle the joint-angle-drift issue, and obtain the synchronous autonomy of a

dual manipulators of redundant robot. Such a solution in^[154] was solved at joint-jerk level making all the joint variables, i.e., joint angles, joint velocities as well as joint accelerations, smooth and bounded. In addition, different types of dynamics algorithms, that is the gradient-type as well as zeroing-type dynamics algorithms, to design the repetitive motion variable vectors, were detailedly shown with circuit schematics. Afterwards, the presented solution in^[154] was formulated into two dynamical QPs, and then integrated into unified dynamical QP for the synchronous autonomy of a dual manipulator of robot system. Note that the optimal solution for UDQP was successfully achieved via a kind of PDNNs. More detailed research by utilizing the PDNNs with application to robot autonomy can also be refereed in the state-of-the-art works.^[155–157]

4. ZNN IN ROBOT AUTONOMY

Remarkably, as a new class of RNNs, Zhang neural networks (or to say, zeroing neural networks, ZNN) can handle problems with multiple state dimensions.^[158] Specifically, such class of RNNs can zero out each element of error function in the neural dynamics manner,^[159] which is thus deemed as a systematic as well as effective methodology to solve different real-time robotic issues.^[160–162] For example, to effectively handle inverse kinematics issue of redundant robots, the redundancy-resolution solutions were investigated in.^[84] The first one was solved at the joint-velocity level, and the second one was solved at the joint-acceleration level. Both the solutions in^[84] were formulated into a dynamical QP. Then, the ZNN was introduced and presented for real-time solution of the related QP. For the purpose of accurate solution of the real-time inverse kinematics issue for the mobile robots, an interesting ZNN is introduced and developed by Xiao and Zhang.^[85] It was theoretically proven that the corresponding model of ZNN in^[85] can globally as well as exponentially converge to the solution of the real-time inverse kinematics problem for mobile robots. Moreover, kinematics equations of a mobile platform as well as a manipulator were integrated as one robot system, and thus the corresponding solution can coordinate simultaneously wheels as well as manipulator to successfully achieve a desired end-effector job. In,^[163] the authors made progress along the direction by introducing a modified zeroing neural network (i.e., the MZNN) model for solving the time-varying QP problem. Note that an original ZNN model and a GNN model are used to compare with the presented MZNN model. Note that detailed theoretical analyses in^[163] prove that the presented MZNN model globally and exponentially converges to the exact real-time solution of the real-time QP without measurement noise. In addition, under the influence of the

measurement noises, such a presented MZNN model would possess a satisfactory performance. Moreover, Jin et al.^[164] presented and investigated an integration-enhanced ZNN and the related model for solving time-varying matrix inversion. Note that theoretical analyses in^[164] prove that the presented integration-enhanced ZNN model possesses the global and exponential convergence property. In addition, under the influence of different kinds of noises, such an integration-enhanced ZNN together with the related model was proven to possess an improved performance. Note that no matter how large the matrix-form constant noise is, such an integration-enhanced ZNN model in^[164] can converge to the theoretical solution. In addition, the residual errors of the presented integration-enhanced ZNN model would be arbitrarily small as for the time-varying noises as well as the random noises. Finally, such an integration-enhanced ZNN model was used to the autonomy problem handling of robots. For the research of discrete-time ZNN, a novel Taylor numerical differentiation formula was introduced for the discretization of the continuous-time ZNN in^[165] to achieve higher computational accuracy. On the basis of such a Taylor numerical differentiation formula, the corresponding Taylor-type discrete-time ZNN models were then introduced and discussed to perform the real-time dynamic equality-constrained QP. For comparison purpose, the Euler-type discrete-time ZNN models as well as the Newton iteration together with their links being found, were also shown in.^[165] It was shown in^[165] that the steady-state residual errors of the presented Taylor-type ZNN models, Euler-type ZNN models, as well as Newton iteration have the patterns of $O(h^3)$, $O(h^2)$, as well as $O(h)$, respectively, with h being the sampling gap. Finally, such a Taylor-type discrete-time ZNN model was applied to the control problem solving of robot manipulators. Moreover, Chen and Zhang^[166] proposed a novel robust ZNN model for handling the inverse kinematics issue of the mobile robots. Differing from most ZNN works on the basis of the assumption that neural networks are free of external disturbances, four common forms of time-varying disturbances suppressed by the presented robust ZNN model were developed in.^[166] Note that theoretical analyses of anti-disturbance performance therein were presented to prove the effectiveness as well as robustness of the presented robust ZNN model with time-varying disturbances suppressed for handling the inverse kinematics issue of mobile robots. In addition, to overcome two major limitations in traditional Jacobian-matrix-pseudo-inverse method, Chen et al.^[167] proposed an interesting Jacobian-matrix-adaptation (JMA) approach for the tracking autonomy of robots via the ZNN design process. Differing from most ZNN works requiring the information of the known robot model, the proposed JMA approach used only

the input-output information to control the robot with unknown model. The solution on the basis of such a JMA approach in^[167] successfully transforms the internal, implicit and unmeasurable model information to the external, explicit as well as measurable input-output information. In,^[168] the authors proposed a novel control method for the controlling knee exoskeleton robot with the real-time inertial and viscous coefficients. Note that the controller was designed on the basis of the ZNN approach and utilized twice Zhang function so as to make the tracking error of joint angle exponentially converge to zero. In,^[135] the authors proposed and investigated a varying-parameter convergent neural dynamic (VP-CND) autonomy approach by exploiting ZNN design approach to stably control the position and attitude angles of an unmanned aerial vehicle (specifically, a flying robot). The proposed VP-CND autonomy approach for the flying robot in^[135] not only can track time-varying desired values but also possesses super-exponential convergence performance. Jin et al.^[133] proposed and developed a distributed solution for the cooperative motion generation in a distributed network of multiple redundant robots (specifically, multirobot system). In order to suppress the noises originating from communication interferences and computational errors, a noise-tolerant ZNN is constructed to solve the QP in real-time. Note that the theoretical as well as the simulative results shown that, in the presence of noise, the proposed distributed scheme in^[133,134] with the aid of noise-tolerant ZNN model has a satisfactory performance.

5. GNN IN ROBOT AUTONOMY

Another special class of RNN, i.e., the GNN, has been introduced and developed as an effective option for the real-time scientific problems handling including the robotics redundancy resolution problem. For example, in 2005, a gradient based neural dynamics system for matrix inversion was revisited by examining different activation functions as well as various implementation errors in.^[107] Then, a general GNN for matrix inversion was thus introduced which was constructed by utilizing the monotonically-increasing odd activation functions. For the aim of superior convergence and robustness of the presented system, the power-sigmoid activation function was preferred to be in use. In addition to investigating the singular case, the reference^[107] also presented an example on inverse kinematic autonomy of redundant robots via real-time pseudo-inverse solution. In 2008, a QP-type method was employed for repetitive motion generation of robot manipulators together with the joint-physical limits considered by Chen et al.^[169] In order to illustrate the effectiveness of such a QP-type repetitive motion generation solution, different kinds of multi-link planar manip-

ulators are used to perform square end-effector trajectories through different simulations. Note that theoretical analysis based on GNN therein was conducted to prove the efficacy of the presented scheme. In 2011, the performance of a GNN, which was developed for handling static problems intrinsically, was introduced as well as analyzed in the situation of time-varying coefficients in.^[111] Specifically, it was theoretically shown that the GNN for real-time solution of time-varying quadratic minimization as well as the corresponding QP problems could only approximately approach the time-varying theoretical solution, instead of converging exactly. In other words, the steady-state error between the GNN solution and the theoretical solution can not decrease to 0. For better understanding the situation, the upper bound of such an error was estimated firstly, and then the global and exponential convergence rate was investigated for such a GNN when approaching the error bound. In 2016, to avoid the Jacobian inversion in the conventional pseudo-inverse solution effectively, and also to achieve the solution of the minimum two-norm position error to the inverse kinematics of the mobile robot, a novel inverse-free solution using the GNN design approach was introduced and developed in.^[170] Note that the inversion of Jacobian matrix is usually required in the pseudo-inverse approach as handling the robotic autonomy problem, which is computationally intensive, especially for the complex mobile robots. By using the advantages of the mutual coordination effect between a mobile platform with two omnidirectional driving wheels and a six-joint manipulator, the integrated kinematics of a robot system was derived and developed therein to coordinate the motions of the platform as well as the manipulator. Moreover, the presented inverse-free solution in^[170] with different values of design parameter as well as the conventional pseudo-inverse solution were conducted for comparison on the basis of the robot system for specific tracking jobs. In addition, Chen and Zhang^[154] proposed a novel jerk-level synchronous repetitive motion solution to address the joint drift problem, and obtain the synchronous autonomy of a dual manipulators of robot system. Note that the corresponding solution was resolved at joint-jerk level making the joint variables, i.e. the joint angles, the joint velocities as well as the joint accelerations,

smooth and bounded. In,^[154] different kinds of dynamics algorithms, i.e. gradient-type (G-type) as well as zeroing-type (Z-type) dynamics algorithms, on the basis of the GNN and the ZNN design approaches respectively, for designing repetitive motion vectors, were shown together with circuit schematics.

6. CONCLUSION

In this review, a comprehensive survey of the research on neural networks in robot autonomy has been presented. Specifically, the state-of-the-art research of RNNs, PDNNs, ZNNs and GNNs in different robot control problems have been detailedly revisited and reported. In addition, the readers and researchers can readily find many referenced solutions on the basis of neural networks for the robot control problem in this review. For future directions of the research on neural networks in robot autonomy, we now provide some prospective outlooks.

- More classes and branches of advanced neural networks would be developed and investigated for solving control problems of robots in different applications.
- The research of complexity, stability and robustness of neural networks would be detailedly investigated during the applications to advanced robots in complex environment.
- The corresponding circuit systems of related neural networks would be developed, implemented and applied to the robot autonomy hardware systems in industry.

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